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# Modifier field strength effects on densification behavior and mechanical properties of alkali aluminoborate glasses

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The constituents of oxide glasses are typically classified as network formers, which form the rigid backbone of glasses, and network modifiers, which tend to either charge stabilize tetrahedral network formers or depolymerize the network. Although it is well known that the properties of glasses depend on their degree of polymerization, little is known about the role of the type of elements used as network modifiers. Here, based on a series of aluminoborate glasses comprising varying alkali oxide modifiers, we show that the glasses' structural and mechanical properties are controlled by the field strength (ratio of charge to size) of the modifiers. Namely, we show that the stiffness, hardness, and toughness depend on a fine balance between the atomic bonding energy, the packing efficiency of the atoms, and the ability of the network to densify reversibly or irreversibly, with each of these features showing a different dependence on the modifier field strength. This opens a new degree of freedom in the optimization of glass properties.

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## I. INTRODUCTION

Oxide glasses are well known to suffer from low practical strength due to the concentration of tensile stresses at the tips of surface flaws and the lack of a stable shearing mechanism capable of dissipating these stresses [1]. This leads to a brittle fracture at some critical stress intensity [2], although some extent of nanoscale ductility has been reported [3,4]. Limiting the tendency to form flaws at the surface, or to initiate cracks from such flaws, would result in improved mechanical performances. Compositional design of new glasses through topological engineering [5] is a promising approach for improving the mechanical properties, as glass compositions can be continuously varied with elements from most of the periodic table due to the lack of stoichiometry requirements [6]. Properties such as hardness, modulus, fracture toughness, as well as cracking pattern vary significantly as a function of chemical composition [7–9], and thus as a function of the inherent structure at the atomic scale. For example, amorphous silica, consisting of fully connected SiO<sub>4</sub> tetrahedral units, forms ring cracks originating at the surface [10,11] when subjected to sharp contact loading (i.e., indentation), as there are significant voids in its network that can facilitate densification, producing high radial tensile stresses at the contact boundary with the indenter [12]. However, upon addition of a modifying oxide (e.g., Na<sub>2</sub>O), the interstices are filled with modifier cations, partly hindering densification and causing the material to deform more by shear flow [12], resulting in median/radial cracking [10]. A larger tendency to deform through shearing can also be obtained by predensifying the glass, which has recently been shown both experimentally and numerically [13–15]. The content of the network modifying oxide is also crucial for the mechanical response of other glassy

frameworks such as borates [16], germanates [17], or mixed network-former glasses [18]. There is thus a large potential for improving mechanical properties such as hardness and toughness of oxide glasses by composition design [19–22]. For instance, we have recently demonstrated that highly damage-resistant aluminoborate glasses can be topologically engineered to exhibit a large extent of densification, which in turn is facilitated by large pressure-induced changes in the chemical environment of the network-forming cations (Al and B) [23,24]. However, to accelerate the search for stronger and more damage-resistant glasses, there is a need to improve the current understanding of how different constituents influence the structure, and in turn the mechanical properties.

In this paper, we investigate the effect of network-modifier type on glass mechanical properties by considering a series of five alkali aluminoborate glasses containing Cs<sub>2</sub>O, Rb<sub>2</sub>O, K<sub>2</sub>O, Na<sub>2</sub>O, or Li<sub>2</sub>O. We study aluminoborate networks due to the limited understanding of mechanical properties in this system, and due to the ease of probing the structural changes of the network-forming Al and B atoms by solid-state nuclear magnetic resonance (NMR) spectroscopy. The compositions in this paper have fixed Al<sub>2</sub>O<sub>3</sub>, B<sub>2</sub>O<sub>3</sub>, and alkali oxide contents, and since all glasses contain monovalent alkali cations the modifiers should exhibit similar roles in the aluminoborate network, i.e., serve to charge balance tetrahedral AlO<sub>4</sub> and BO<sub>4</sub> units. However, due to the difference in the alkali size, their ability to charge balance differs, as the same charge is distributed over a larger area for larger cations. This is conveniently quantified by the modifier field strength (FS), as defined by Dietzel [25]:

$$FS = \frac{z_{\text{alkali}}}{(r_{\text{alkali}} + r_{\text{oxygen}})^2}, \quad (1)$$

where  $z$  and  $r$  are the charge and the ionic radius, respectively. Higher FS modifier cations are known to form stronger bonds

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with oxygen [26], which should result in higher hardness and modulus [7,27,28]. It has also been found that increasing the FS of the modifier yields a higher indentation fracture toughness [29,30], but the underlying structural origin of this behavior is not yet fully understood. Here, we report on the effect of substituting the alkali oxide type on hardness, elastic moduli, toughness, and extent of indentation cracking in an aluminoborate glass, in order to clarify the role of the modifier FS in controlling the mechanics of crack-resistant glasses. We compare the trends in mechanical properties with the glasses' tendency to densify when subjected to (i) isostatic compression at elevated temperature (hot compression) and (ii) localized indentation-induced densification at room temperature. The correlations between FS and mechanical properties are discussed using the structural information obtained from  $^{11}\text{B}$  and  $^{27}\text{Al}$  magic angle spinning (MAS) NMR spectroscopy experiments. As such, this paper helps to facilitate the design of new glass materials with tailored mechanical performances. In future work, we will investigate aluminoborate glasses with divalent alkaline earth modifier cations to check the generality of the observed trends in mechanical properties with FS.

## II. EXPERIMENTAL SECTION

### A. Sample preparation

The nominal glass compositions introduced in this paper are in the  $25M_2\text{O}-20\text{Al}_2\text{O}_3-55\text{B}_2\text{O}_3$  system with  $M = \text{K, Rb, and Cs}$ . The preparation procedures for glasses with  $M = \text{Na and Li}$  are described elsewhere [23,24]. The glasses with  $M = \text{K, Rb, and Cs}$  were prepared by mixing appropriate amounts of the precursors ( $\text{K}_2\text{CO}_3$ ,  $\text{Rb}_2\text{CO}_3$ ,  $\text{Cs}_2\text{CO}_3$ ,  $\text{Al}_2\text{O}_3$ , and  $\text{H}_3\text{BO}_3$ ), and melting them in Pt-Rh crucibles at 1200–1300 °C depending on the composition. The final melts were quenched onto a brass plate and annealed around their glass transition temperature ( $T_g$ ) estimated from the data for Li- and Na-aluminoborate glasses [23,24]. The chemical compositions were determined through flame emission and inductively coupled plasma optical emission spectroscopy techniques (Table I).

The  $T_g$  values were determined using differential scanning calorimetry (DSC) measurements (DSC 449C, Netzsch) from the intercept between the extrapolated isobaric heat capacity of the glass ( $C_p$ ) and the tangent to the inflection point recorded during the glass transition for 40-mg specimens with a specific thermal history (obtained by controlled cooling in the DSC at 10 K/min).  $C_p$  vs  $T$  curves were acquired from a

sapphire-calibrated energy output from the DSC. Each bulk glass specimen was then annealed at its measured  $T_g$  for 1 h, and cooled at 3 K/min. The glasses were confirmed to be amorphous using x-ray diffraction (Empyrean XRD, PANalytical) on powdered samples.

Samples of all glasses were cut into desired dimensions ( $\sim 15 \times 15 \times 3 \text{ mm}^3$ ) for density, indentation, and hot compression experiments [31]. The high-pressure treatment was carried out for all studied compositions by maintaining the specimens at their respective  $T_g$  in an  $\text{N}_2$  atmosphere at 1.0 GPa for 30 min, and quenching from those conditions with an initial cooling rate of approximately 60 K/min. The high-pressure setup is described in detail elsewhere [31].

### B. NMR spectroscopy

Na, K, Rb, and Cs glasses were subjected to  $^{11}\text{B}$  and  $^{27}\text{Al}$  MAS NMR experiments, while the results for the Li glass are taken from Ref. [24]. Spectra were acquired with commercial spectrometers (VNMRs, Agilent) and 3.2-mm MAS NMR probes (Agilent), using an external magnetic field of 16.4 T. The detailed experimental procedures can be found in Ref. [24]. Fitting of  $^{27}\text{Al}$  MAS NMR spectra to extract Al speciation for each of the glasses was performed using DMFit [32] and the CzSimple model, accounting for distributions in the quadrupolar coupling constant. Q MAS  $\frac{1}{2}$  and Gaus/Lor functions were used for fitting of  $^{11}\text{B}$  MAS NMR spectra, also with DMFit.

### C. Density

Density ( $\rho$ ) was determined for both the as-prepared and the compressed glass specimens using the Archimedes principle of buoyancy with ethanol as the immersion fluid. Each specimen, weighing at least 1 g, was weighed in air and in liquid, ten times each, and the density was calculated as

$$\rho_{\text{glass}} = \frac{m_{\text{air}}}{(m_{\text{air}} - m_{\text{liquid}})}(\rho_{\text{liquid}} - \rho_{\text{air}}) + \rho_{\text{air}}. \quad (2)$$

Plastic compressibility ( $\beta$ ), i.e., the permanent increase in density, is determined from the initial and final density values and the applied pressure ( $P$ ) value:

$$\beta = \frac{\rho_{\text{final}} - \rho_{\text{initial}}}{\rho_{\text{initial}} \cdot P}. \quad (3)$$

TABLE I. Analyzed chemical compositions, glass transition temperature ( $T_g$ ), density ( $\rho$ ), molar volume ( $V_s$ ), and atomic packing density ( $C_g$ ) of the as-prepared glasses. The plastic compressibility ( $\beta$ ) following hot compression is also given. The errors in  $T_g$ ,  $\rho$ ,  $V_s$ ,  $C_g$ , and  $\beta$  do not exceed  $\pm 2^\circ\text{C}$ ,  $\pm 0.001 \text{ g/cm}^3$ ,  $\pm 0.02 \text{ cm}^3/\text{mol}$ ,  $\pm 0.001$ , and  $\pm 0.002 \text{ GPa}^{-1}$ , respectively.

Glass ID	[M <sub>2</sub> O] (mol %)	[Al <sub>2</sub> O <sub>3</sub> ] (mol %)	[B <sub>2</sub> O <sub>3</sub> ] (mol %)	$T_g$ (°C)	$\rho$ (g/cm <sup>3</sup> )	$V_m$ (cm <sup>3</sup> /mol)	$C_g$	$\beta$ (GPa <sup>-1</sup> )
Li <sup>a</sup>	24.1	20.9	55.1	478	2.241	29.52	0.545	0.081
Na <sup>b</sup>	25.5	20.4	54.1	451	2.240	33.11	0.510	0.061
K	22.8	21.7	55.5	429	2.170	37.90	0.498	0.054
Rb	24.0	20.7	55.3	417	2.595	40.63	0.492	0.058
Cs	24.8	19.9	55.3	416	2.886	44.75	0.479	0.072

<sup>a</sup>Data are taken from Ref. [24].

<sup>b</sup>Data are taken from Ref. [23].

#### D. Indentation

All as-prepared and compressed specimens for indentation analyses were ground using SiC adhesive discs, and polished in water-free diamond suspensions to avoid hydration of the surface. Microindentation measurements (Duramin 5 microindenter, Struers) were performed using the Vickers-type geometry at ambient temperature and relative humidity of  $44 \pm 4\%$ . Thirty identical indentations at 19.6-N press load and 10-s holding time were performed for each specimen. Cracks emanating from the corners of the indents were counted and their lengths from the center of the indents ( $c$ ) were measured approximately 1 min after unloading. Vickers hardness ( $H_V$ ) was calculated from the applied load ( $P$  in newton) and the average half length of the diagonals ( $a$  in  $\mu\text{m}$ ) measured on the residual imprint visible under the optical microscope attached to the microindenter:

$$H_V = \frac{1854.4P}{a^2}. \quad (4)$$

In addition, ten indents loaded at 245 mN were subjected to an analysis of the deformation mechanism, as suggested in Ref. [33]. An atomic force microscope (AFM, Ntegra, NT-MDT) was utilized to determine the topography of each indent both before and after a 2-h annealing cycle at  $0.9 T_g$  (temperature in Kelvin). Silicon tip cantilevers (NSG10, NT-MDT) were used in semicontact mode to record  $20 \times 20$ - or  $25 \times 25$ - $\mu\text{m}^2$  images at  $\sim 0.5$ -Hz scanning frequency. The acquired images with a  $256 \times 256$ -pixel resolution were then used to determine the indentation and pile-up volumes ( $V_i^-$  and  $V_i^+$ , respectively) for the initial indent, and the corresponding volumes after thermal relaxation ( $V_a^-$  and  $V_a^+$ ). The extent of densification is then quantified through the volume recovery ratio ( $V_R$ ), which corresponds to the fraction of the indentation volume  $V_i^-$  that is due to densification.  $V_R$  is calculated as in Ref. [33]:

$$V_R = \frac{(V_i^- - V_a^-) + (V_a^+ - V_i^+)}{V_i^-}. \quad (5)$$

In order to probe the glasses' elastic response to indentation, a Nano Indenter XP (MTS) equipped with a Berkovich geometry diamond tip was used to record at least ten loading-unloading cycles for a subset of the specimens. The applied load ( $P$ ) and the displacement ( $h$ ) were continuously monitored during the loading, the 10-s hold, and the unloading segments of each measurement cycle. The target  $d$  was 2000 nm. According to the Oliver-Pharr methodology [34], hardness ( $H_{\text{nano}}$ ) was assessed from the projected contact area ( $A_c$ ) of the indent [Eq. (6)], and the reduced indentation modulus ( $E_r$ ) was calculated from the top 1/3 of the unloading  $P/h$  curve [Eq. (7)]. The indentation modulus ( $E_{\text{IT}}$ ) was then calculated from  $E_r$  and the elastic properties of the indenter material, i.e., diamond [Eq. (8)]:

$$H_{\text{nano}} = \frac{P}{A_c}, \quad (6)$$

$$E_r = \frac{1}{2} \frac{dP}{dh} \sqrt{\frac{\pi}{A_c}}, \quad (7)$$

$$E_{\text{IT}} = \left( \frac{1}{E_r} - \frac{1 - \nu_{\text{ind}}^2}{E_{\text{ind}}} \right)^{-1}. \quad (8)$$

In Eq. (7),  $dP/dh$  corresponds to the material stiffness recorded during unloading of the indenter. In Eq. (8),  $\nu_{\text{ind}}$  and  $E_{\text{ind}}$  correspond to  $\nu$  and  $E$  of diamond.

#### E. Elastic moduli

An ultrasonic thickness gauge (38DL Plus, Olympus) was used to acquire the longitudinal and transverse wave velocities ( $V_L$  and  $V_T$ , respectively) in the glass specimens using the pulse-echo method. The thickness of the samples was measured with a digital micrometer. Delay line transducers of 20 MHz were used to induce the longitudinal and transverse waves. Shear modulus ( $G$ ), Young's modulus ( $E$ ), and Poisson's ratio ( $\nu$ ) were calculated using the recorded  $V_L$  and  $V_T$ , and the density of the glass specimens according to Eqs. (9)–(11):

$$G = \rho V_T^2, \quad (9)$$

$$\nu = \frac{V_L^2 - 2V_T^2}{2(V_L^2 - V_T^2)}, \quad (10)$$

$$E = 2G(1 + \nu). \quad (11)$$

### III. RESULTS AND DISCUSSION

#### A. Boron and aluminum speciation

In the studied glasses, both Al and B can attain different coordination numbers with oxygen, depending on the chemical composition [35,36], as well as thermal and pressure history [23]. Network-forming Al and B cations coordinated with more than three oxygen anions require a network modifier (e.g., alkali cation) to maintain charge neutrality. An increase in oxygen coordination number manifests itself in larger shielding of the nuclei when probed by MAS NMR spectroscopy, giving rise to additional resolvable signals upfield. The  $^{11}\text{B}$  and  $^{27}\text{Al}$  MAS NMR spectra (Fig. 1) of the investigated glasses show pronounced differences in the chemical environments for both B and Al. The majority of boron atoms are in threefold coordination ( $\text{B}^{\text{III}}$ ), with some four-coordinated sites ( $\text{B}^{\text{IV}}$ ) present as well. Aluminum atoms exist almost exclusively in fourfold coordination ( $\text{Al}^{\text{IV}}$ ), with the exception of the Li glass, which has substantial fractions of five- ( $\text{Al}^{\text{V}}$ ) and sixfold coordinated ( $\text{Al}^{\text{VI}}$ ) species.

Spectral deconvolution performed using DMFit [32] allows us to extract the relative populations of each site (Table II), showing that the connectivity of the glasses is sensitive to the FS of the network modifier. A local minimum in the average coordination number of boron ( $\langle n_B \rangle$ ) as a function of FS is found for the K glass (Fig. 2). However, given the experimental error in  $\langle n_B \rangle$  ( $\pm 0.01$ ) and the discrepancy in the nominal vs analyzed composition (the molar percentage of  $\text{K}_2\text{O}$  is the smallest, Table I), it is likely that boron speciation is approximately constant at low FS and then increases dramatically for the smaller Na and Li cations. Similarly, the aluminum speciation is not subject to significant changes as a function of FS, with the exception of the Li glass (Fig. 2). The difference in the structure of the Li glass



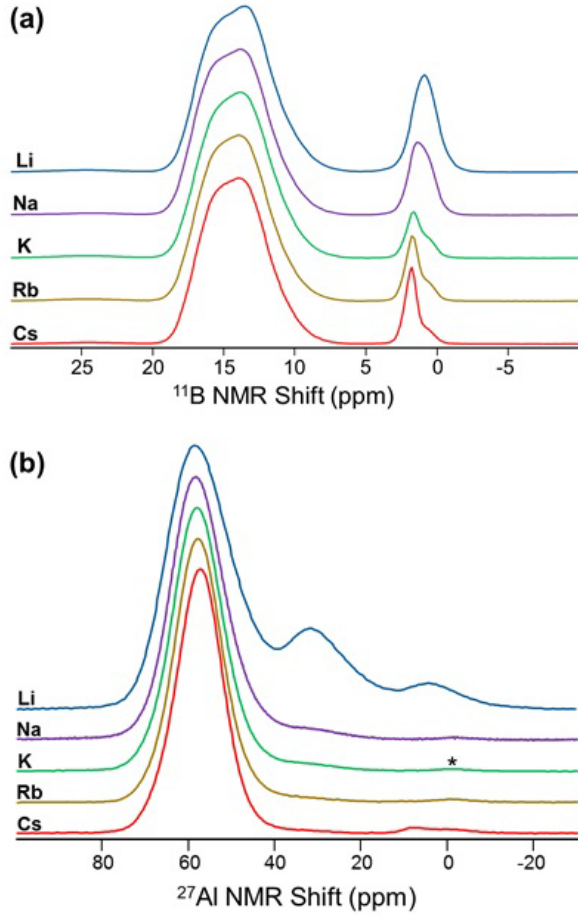


FIG. 1. (a)  $^{11}\text{B}$  and (b)  $^{27}\text{Al}$  MAS NMR spectra for the investigated glasses. Data for Li glass are taken from Ref. [24]. The small peak marked by \* is due to background signal from the zirconia rotor.

compared to the other lower-FS glasses could be related to the preference for modifiers to charge balance  $\text{Al}^{\text{IV}}$  vs  $\text{B}^{\text{IV}}$  units. That is, in alkali aluminoborate glasses, B and Al tetrahedra compete for the charge-balancing alkali cation, with a well-known preference for alkali- $\text{Al}^{\text{IV}}$  association [35]. However, previous studies [37,38] suggest that the extent of disorder in oxide glasses increases with increasing FS, suggesting a more random association of different network modifiers and formers. As such, our results suggest that the

TABLE II. Fractions of three- and four-coordinated boron species ( $\text{B}^{\text{III}}$  and  $\text{B}^{\text{IV}}$ ), as well as four-, five-, and six-coordinated aluminum species ( $\text{Al}^{\text{IV}}$ ,  $\text{Al}^{\text{V}}$ , and  $\text{Al}^{\text{VI}}$ , respectively) determined from MAS NMR experiments. The errors in fractions do not exceed 1 and 2% for boron and aluminum fractions, respectively.

Glass ID	$\text{B}^{\text{III}}$ (%)	$\text{B}^{\text{IV}}$ (%)	$\text{Al}^{\text{IV}}$ (%)	$\text{Al}^{\text{V}}$ (%)	$\text{Al}^{\text{VI}}$ (%)
Li <sup>a</sup>	84	16	73	23	4
Na	88	12	97	3	0
K	94	6	95	4	1
Rb	92	8	95	4	1
Cs	92	8	97	1	2

<sup>a</sup>Data are taken from Ref. [24].

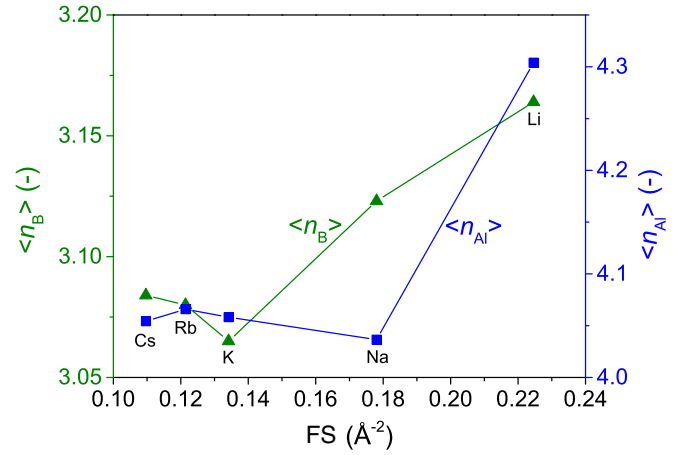


FIG. 2. Alkali field strength (FS) dependence of the average B coordination number ( $\langle n_{\text{B}} \rangle$ , green triangles) and Al coordination number ( $\langle n_{\text{Al}} \rangle$ , blue squares). Data for Li glass are taken from Ref. [24]. The errors in  $\langle n_{\text{B}} \rangle$  and  $\langle n_{\text{Al}} \rangle$  do not exceed 0.01 and 0.02, respectively.

preference for  $\text{Li}^+$  to associate with  $\text{Al}^{\text{IV}}$  over  $\text{B}^{\text{IV}}$  units is low compared with the lower-FS glasses. In other words,  $\text{Li}^+$  cations appear to be more randomly distributed throughout the network, which explains the large fraction of  $\text{B}^{\text{IV}}$  units for  $M = \text{Li}$  compared with the other glasses. As a result, a higher fraction of Al atoms must attain a network-modifying role as  $\text{Al}^{\text{V}}$  and/or  $\text{Al}^{\text{VI}}$  units.

It should also be noted that the alkali FS depends on the glass composition, as the alkali coordination number with oxygen depends on its chemical environment. In turn, the coordination number affects its ionic radius, which is used in the calculation of FS [Eq. (1)]. In this paper, we have assumed the coordination number of all alkali cations to be 6. A detailed structural study would be necessary to determine the actual coordination number for all the studied glasses, but this would be outside the scope of the present paper. However, we note that lighter alkali elements tend to have lower coordination numbers, while heavier ones generally display higher coordination numbers [39]. If we consider this in the calculation of FS, the differences in FS between the five alkali metals would actually increase. As such, the trend presented in Fig. 2 (and in the subsequent figures) remains qualitatively correct despite the assumption of sixfold coordination with oxygen for all alkali ions.

## B. Glass transition temperature and density

The effect of the modifier field strength on the glass transition temperature is illustrated in Fig. 3, revealing an increase in  $T_g$  with increasing FS. According to the NMR data, substituting  $\text{Li}_2\text{O}$  for  $\text{Na}_2\text{O}$  results in more atomic constraints per atom (higher connectivity), i.e., a more rigid glass network that could result in a higher  $T_g$  [40]. However, the network connectivity is not a linear function of FS for the lower-FS glasses (Fig. 2), i.e., the monotonic increase in  $T_g$  with increasing FS is not only determined by the average coordination numbers of Al and B. In addition, the difference in the strength of the constraints associated with

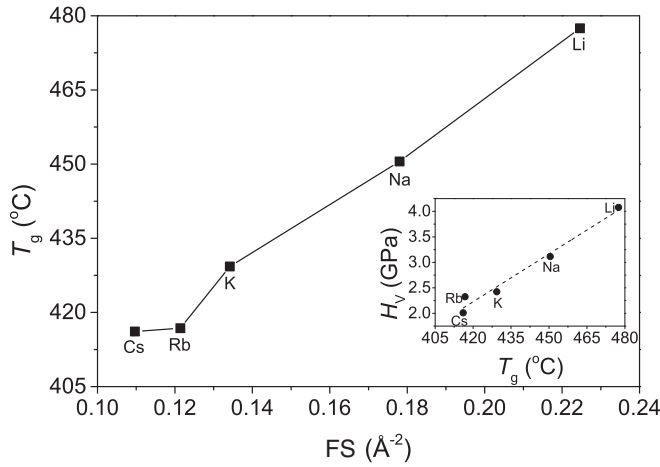


FIG. 3. Alkali field strength (FS) dependence of the glass transition temperature ( $T_g$ ). Data for Li and Na glasses are taken from Refs. [23,24]. Inset: Correlation between  $T_g$  and Vickers hardness ( $H_V$ ). The errors in  $T_g$  and  $H_V$  do not exceed  $\pm 2^\circ\text{C}$  and  $\pm 0.1\text{ GPa}$ , respectively.

the alkali-oxygen bonds should be considered [41]. Namely, high-FS alkali cations generally form stronger bonds with oxygen [7,42], in agreement with the positive correlation between FS and  $T_g$  in Fig. 3.

The room-temperature density and thus molar volume ( $V_m$ ) of the as-prepared glasses are also strongly dependent on the alkali oxide added to the aluminoborate network (Table I). The heavy alkali elements like Cs and Rb are expected to yield a relatively high-density glass given their large mass and indeed the density initially decreases with increasing FS (Fig. 4). However, as  $\text{Na}_2\text{O}$  is substituted for  $\text{K}_2\text{O}$ , the density increases despite the fact that Na is lighter than K. This suggests that the observed trend in the density might result from a balance between the atomic weight of the modifiers and the efficiency of their local packing. The atomic packing efficiency increases with the FS. Considering the constituent atoms as spheres

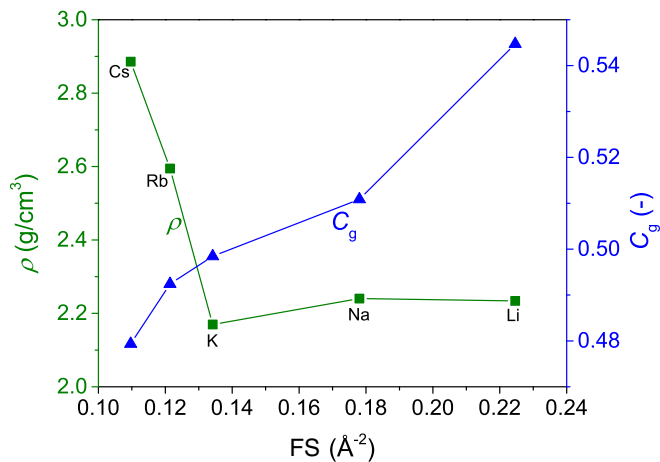


FIG. 4. Alkali field strength (FS) dependence of density ( $\rho$ , green squares) and atomic packing density ( $C_g$ , blue triangles). Data for Li and Na glasses are taken from Refs. [23,24]. The errors in  $\rho$  and  $C_g$  are smaller than the size of the symbols.

with a known ionic radius [43], one can determine the atomic packing density ( $C_g$ ). Assuming sixfold coordination for all alkali cations, twofold coordination for oxygen anions, and three- to sixfold coordination for B and Al atoms based on the NMR data,  $C_g$  can be calculated as

$$C_g = \frac{\rho \sum f_i [4/3\pi N (x r_A^3 + y r_B^3)]}{\sum f_i M_i}, \quad (12)$$

where for the  $i$ th constituent with chemical formula  $A_x B_y$ ,  $f_i$  is the molar fraction,  $r_A$  and  $r_B$  are the ionic radii,  $M_i$  is the molar mass, and  $N$  is Avogadro's number.  $C_g$  is indeed found to increase with increasing modifier FS (Fig. 4). The local minimum in density can be explained from the fact that (i) smaller modifiers can more efficiently fill the voids left between O atoms, thereby reducing the amount of internal free volume, and (ii) modifiers exhibiting large FS tend to attract more the surrounding O atoms, thereby forcing them to partially overlap with each other. This is consistent with recent molecular dynamics simulations showing that the O atoms around network formers (i.e.,  $\text{FS} > 1.3 \text{ \AA}^{-2}$ ) are experiencing a compressive state due to the strong attraction from the central cation [44].

The observed dependence of  $T_g$  and  $C_g$  on the modifier field strength therefore suggests that when the low-FS  $\text{Cs}_2\text{O}$  modifies the aluminoborate network the glass is relatively loosely packed and the individual bonds are weak. However, when the high-FS  $\text{Li}_2\text{O}$  is used as a modifier, the structure is more rigid and tightly packed with stronger alkali-oxygen bonds.

### C. Hardness and elasticity

Vickers microindentation of the glasses at 19.6-N load results in square-shaped indent impressions in their surfaces, as illustrated in the inset of Fig. 5(a). According to Eq. (4), the diagonal lengths [marked by green lines in the inset of Fig. 5(a)] and the applied load are used to determine the Vickers hardness ( $H_V$ ), i.e., the glass's resistance to elastoplastic deformation. Increasing the FS of the alkali cation has a positive influence on  $H_V$  of the aluminoborate glasses as  $H_V$  increases from  $\sim 2$  to  $\sim 4\text{ GPa}$  when  $\text{Li}_2\text{O}$  is substituted for  $\text{Cs}_2\text{O}$  [Fig. 5(a)]. A similar trend was recorded for  $T_g$  (Fig. 3), implying that both of these properties have similar structural origin (inset of Fig. 3). Indeed, both  $T_g$  and  $H_V$  have been linked to the number of atomic constraints per atom, defining the rigidity of the glass network [22,45]. Considering here the lack of a linear increase in coordination numbers of the network-forming cations (B and Al) as a function of increasing FS of the alkali cation, we infer that the rigidity of the aluminoborate glasses is sensitive to the modifier constraints.  $H_V$  of the glass samples compressed at 1 GPa at their respective ambient pressure  $T_g$  values has also been determined (Table III). In agreement with previous work on predensified glasses,  $H_V$  increases with increasing applied pressure and thus degree of densification [46]. The magnitude of the hardness increase scales positively with the extent of pressure-induced density increase (Table III).

In addition to Vickers microindentation, the glasses have also been subjected to depth-sensing instrumented nanoindentation. Equation (6) is used to compute  $H_{\text{nano}}$  using the information extracted from the unloading part of the

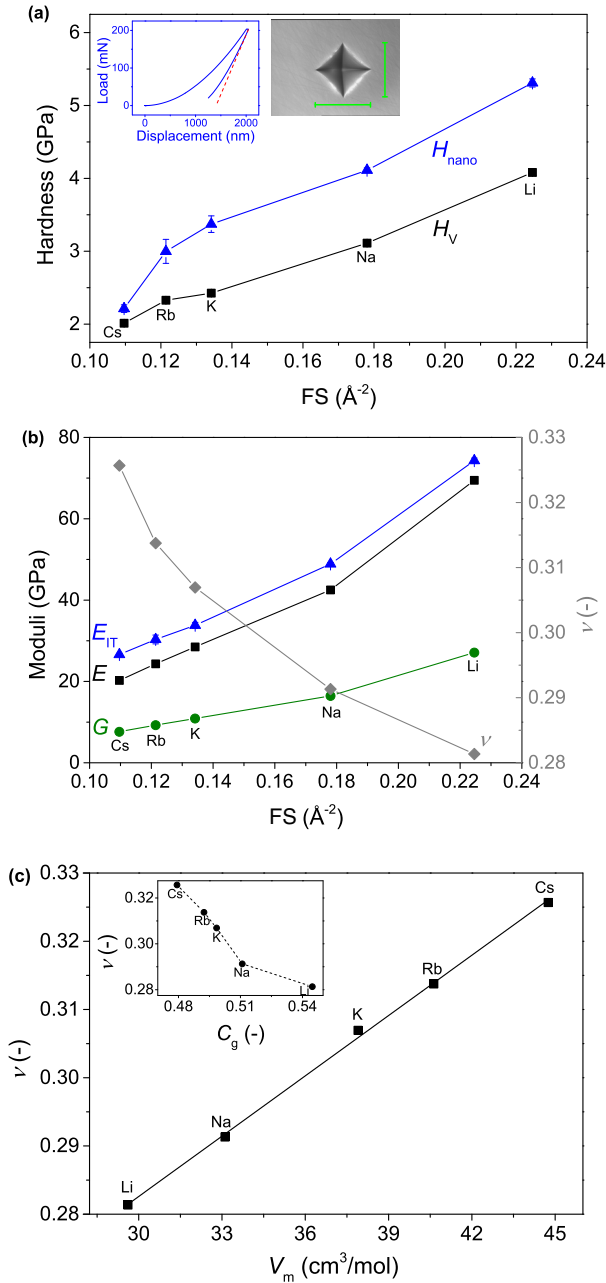


FIG. 5. (a) Alkali field strength (FS) dependence of Vickers hardness ( $H_V$ , black squares) and nanohardness ( $H_{\text{nano}}$ , blue triangles). Insets: Load-displacement curve extracted from nanoindentation and optical microscopy image of a Vicker's indent used to calculate  $H_{\text{nano}}$  [Eq. (6)] and  $H_V$  [Eq. (4)], respectively. (b) FS dependence of Young's modulus ( $E$ , black squares), shear modulus ( $G$ , green circles), indentation modulus ( $E_{IT}$ , blue triangles), and Poisson's ratio ( $\nu$ , gray diamonds). (c) Correlation between  $\nu$  and molar volume ( $V_m$ ) and  $C_g$  (inset). Data for Li and Na glasses are taken from Refs. [23,24]. Errors in  $H_{\text{nano}}$ ,  $H_V$ ,  $E$ ,  $G$ ,  $E_{IT}$ , and  $\nu$  do not exceed 0.2 GPa, 0.1 GPa, 2 GPa, 1 GPa, 2 GPa, and 0.015 respectively.

load-displacement curves [see example in the inset of Fig. 5(a)]. The compositional scaling of  $H_{\text{nano}}$  resembles that of  $H_V$ . Nanoindentation also provides insight into the elastic recovery of the glass. By considering the unloading part of the load-displacement curve, the indentation modulus ( $E_{IT}$ ) can be

determined using Eqs. (7)–(9). Similarly to the trends observed for  $T_g$ ,  $H_V$ , and  $H_{\text{nano}}$ , we find a positive linear correlation between  $E_{IT}$  and the FS of the modifying alkali cation [Fig. 5(b)].

The compositional trend in  $E_{IT}$  is similar to that observed in Young's modulus ( $E$ ) as measured using the ultrasonic echography method [Fig. 5(b)]. However, the absolute values tend to differ slightly, especially for the low-FS alkali glasses. This is likely due to an overestimation of  $E_{IT}$ , which is frequently ascribed to formation of pile-up during indentation [47]. The shear modulus ( $G$ ) exhibits a similar dependence on FS as  $E$  and  $E_{IT}$  [Fig. 5(b)]. We should note that  $E$  and  $G$  for the Li glass have been measured using Brillouin scattering [24], i.e., the absolute values for the investigated glasses may not be directly comparable, but the positive correlation between elastic moduli and FS is clearly confirmed. Furthermore, the increases in the elastic moduli due to hot compression correspond well to the observed increases in density (Table III) [48].

In addition to the magnitude of resistance to elastic deformation, the ultrasonic echography method can be used to determine Poisson's ratio ( $\nu$ ), which has been found to be an important metric for understanding the mechanical properties of glasses [49]. For the present alkali aluminoborate glasses,  $\nu$  decreases with increasing FS [Fig. 5(b)]. Furthermore, we find that  $\nu$  increases linearly with  $V_m$  [Fig. 5(c)]. This suggests that open aluminoborate glass networks exhibit higher  $\nu$ . This is unexpected as there is generally a positive correlation between packing efficiency ( $C_g$ ) and  $\nu$  when considering different glass systems [8], but here we observe the opposite trend [inset of Fig. 5(c)]. Materials with a closely packed structure (i.e., high  $C_g$  and low  $V_m$ ) should exhibit small volume changes when changing shape, since there is limited room for densification, which should in turn manifest itself in a high  $\nu$  value. However, this explanation does not appear to hold for the present aluminoborate glasses. Rouxel [8] has argued that  $\nu$  also depends on the dimensionality of the material, which is dictated by the connectivity. That is, for low-connectivity glasses like amorphous Se, it is easy for the atoms to rearrange upon loading and thus for the material to expand laterally during longitudinal compression. On the other hand, glasses exhibiting high connectivity are more rigid and cannot easily rearrange and will tend to store some internal stress rather than reorganizing on the direction normal to the load. However, considering the NMR data for the studied glasses, the aluminum and boron speciations are roughly constant at low FS values (Fig. 2). The trend in connectivity can therefore only partially explain the negative correlation between  $C_g$  and  $\nu$ . We thus infer that the unexpected FS dependence of  $\nu$  [Fig. 5(b)] is a result of the varying strength of the alkali-oxygen bond constraints, which are expected to increase with FS along with the increasing dissociation energy of the alkali-oxygen bonds [7,26,42]. Hence, for the alkali aluminoborates studied here, the lowest  $\nu$  values are found in glasses with the weakest bonds, and not in glasses with the highest  $C_g$  as shown in other systems [8].

#### D. Densification upon hot compression

Next we investigate the glasses' tendency to densify upon hot compression. The extent of densification is quantified

TABLE III. Vickers hardness at 19.6 N ( $H_V$ ), nanohardness ( $H_{\text{nano}}$ ), indentation modulus ( $E_{\text{IT}}$ ), Young's modulus ( $E$ ), shear modulus ( $G$ ), and Poisson's ratio ( $\nu$ ) of the as-prepared and hot compressed (at 1 GPa) glasses. The errors in  $H_V$ ,  $H_{\text{nano}}$ ,  $E_{\text{IT}}$ ,  $E$ ,  $G$ , and  $\nu$  do not exceed  $\pm 0.1$  GPa, 0.2 GPa, 2 GPa, 2 GPa, 1 GPa, and 0.015, respectively.

	$H_V$ (GPa)	$H_{\text{nano}}$ (GPa)	$E_{\text{IT}}$ (GPa)	$E$ (GPa)	$G$ (GPa)	$\nu$	$H_V$ (GPa)	$H_{\text{nano}}$ (GPa)	$E_{\text{IT}}$ (GPa)	$E$ (GPa)	$G$ (GPa)	$\nu$
Glass ID	As-prepared						Compressed					
Li <sup>a</sup>	4.1	5.3	74	69	27	0.281	5.9	7.6	99	90	35	0.274
Na <sup>b</sup>	3.1	3.4	49	43	17	0.291	4.1	4.4	64	55	22	0.286
K	2.4	2.6	34	29	11	0.307	3.3			38	15	0.297
Rb	2.3	2.5	30	24	9	0.314	3.0			32	12	0.307
Cs	2.0	2.2	27	20	8	0.326	2.8			27	10	0.319

<sup>a</sup>All data are taken from Ref. [24].

<sup>b</sup> $H_V$ ,  $H_{\text{nano}}$ , and  $E_{\text{IT}}$  data are taken from Ref. [23].

through the plastic compressibility [ $\beta$ , Eq. (3)]. As shown in Fig. 6(a), there is no monotonic correlation between  $\beta$  and FS. That is,  $\beta$  exhibits a pronounced minimum around the K glass. This suggests that two competing deformation mechanisms are at play. The high  $\beta$  value of the low-FS Cs glass could be due to its relatively low  $C_g$  value (Fig. 4), resulting in a large potential for densification achieved by local compaction of the network atoms with only limited changes in the next-nearest-neighbor environment. In other words, we infer that densification of the low-FS glasses is dominated by medium-range order

reorganization. Upon increasing the FS through substitution of  $\text{K}_2\text{O}$  for  $\text{Cs}_2\text{O}$ ,  $C_g$  also increases (Fig. 4), which likely requires more significant changes in the short-range order of the network in order to allow for further compaction of the atoms, thus causing  $\beta$  to decrease initially as a function of FS. However, as FS increases further when the size of the modifying cation becomes even smaller (i.e., substitution of  $\text{Li}_2\text{O}$  for  $\text{K}_2\text{O}$ ), the ability of the cations to charge stabilize adjacent boron and aluminum tetrahedra at high pressure is improving given that smaller cations occupy less space around those tetrahedral units [50]. This hypothesis is supported by our previous work concerning the self-adaptivity of the Li- vs Na-containing aluminoborate glasses [23,24]. More specifically, the pressure-induced increase in the coordination number of both B and Al is higher for the Li glass compared to the Na glass, indicating that  $\text{Li}^+$  ions enable more permanent densification through structural transformations in the short-range order. Hence, we suggest that the increase in  $\beta$  with increasing FS is due to the smaller pressure-driven resistance to changes in glass connectivity at high FS.

### E. Indentation deformation mechanism

The structural reasoning for the composition dependence of densification upon hot compression suggested above could also hold for that of densification upon sharp contact loading. However, the trend in  $V_R$  is opposite that of  $\beta$  [Fig. 6(a)], suggesting that the Li glass has a higher resistance to indentation densification. As we discuss in detail below, this may be due to the large differences among the glasses in their elastic response to indentation, which strongly affects the initial indentation volume,  $V_i^-$ . We should note that we are not able to correctly determine the  $V_R$  value of the Cs glass, as it exhibits an anelastic response or alternatively corrosion of the indented zone [Fig. 6(b)], resulting in an underestimation of  $V_i^-$ . The volumes used to calculate  $V_R$  for the other glasses are given in Table IV.

To obtain information of the glasses' elastic recovery, we here consider the bow-in of the indent faces upon unloading, which exhibits clear composition dependence. Figure 7(a) illustrates the recorded AFM images of the investigated glasses (with the exception of Cs glass due to the same reason as stated above). By measuring the indent diagonal length ( $L_D$ ) and the opposite side length ( $L_S$ ), the elastic response of the material

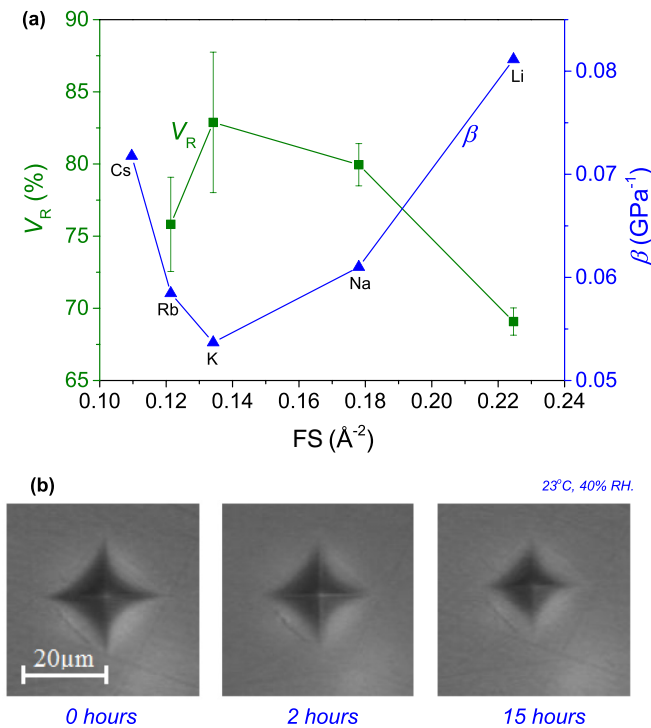


FIG. 6. (a) Alkali field strength (FS) dependence of volume recovery ratio ( $V_R$ , green squares) and plastic compressibility ( $\beta$ , blue triangles).  $V_R$  of the Cs glass could not be determined as explained in the text. Data for Li and Na glasses are taken from Refs. [23,24]. (b) Indentation imprint at 0.98 N in the Cs glass recorded immediately after unloading or after exposure to ambient atmosphere for 2 and 15 h.



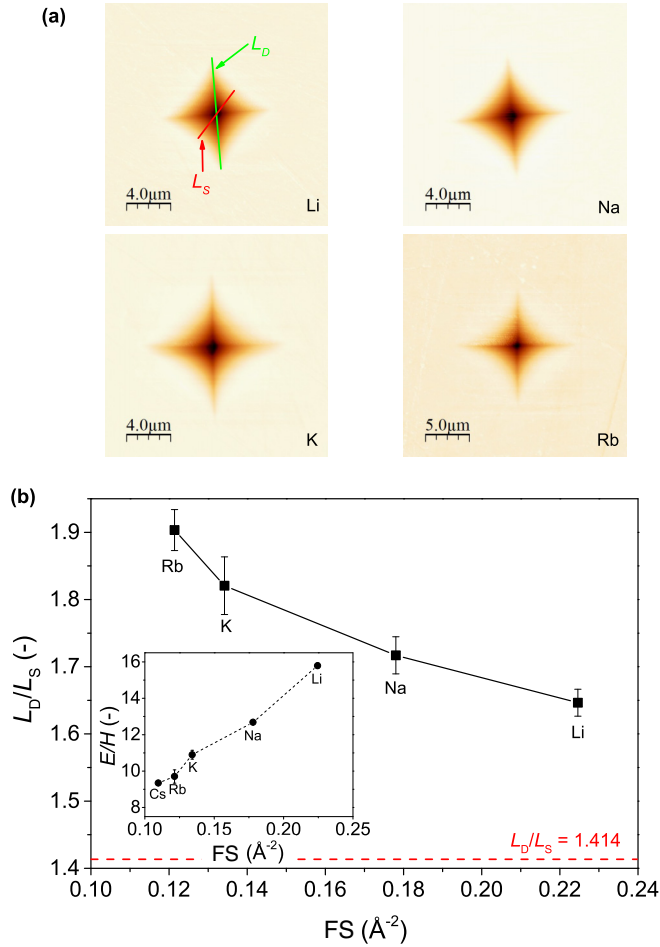


FIG. 7. (a) Atomic force microscopy images of indentation imprints produced at 0.25 N in Li, Na, K, and Rb glasses. The determination of the diagonal length ( $L_D$ ) and the opposite side length ( $L_S$ ) is illustrated. (b) Alkali field strength (FS) dependence of the bow-in parameter  $L_D/L_S$ . The dashed line represents the theoretical minimum  $L_D/L_S$  value (i.e., the case with no bow-in). Inset: FS dependence of the elastoplastic ratio ( $E/H$ ).

surrounding the indentation-induced cavity can be quantified by calculating the  $L_D/L_S$  ratio [51]. We find a negative correlation between  $L_D/L_S$  and FS [Fig. 7(b)]. As such, the Li glass has the lowest  $L_D/L_S$  ratio and therefore experiences the least elastic recovery during unloading. This is consistent with the trend in elastoplastic ratio  $E/H$  [inset of Fig. 7(b)], which also describes the extent of elastic contribution to indentation [52].

The topographic maps of the indent impressions also allow us to estimate the volume fraction of elastic recovery by comparing the postunloading indentation volume ( $V_i^-$ ) to the theoretical volume of the indenter during full loading ( $V_G$ ).  $V_G$  can be calculated from the indent diagonals due to the known geometry of the Vickers pyramid under the assumption that the displacement of corners of the indentation impression during unloading is negligible. The elastic contribution to the total indentation volume ( $V_E$ ) can then be calculated as  $1 - V_i^-/V_G$ . Using the same approach, we also calculate the densification and shear flow volume fractions ( $V_D$  and  $V_S$ , respectively) using the volumes determined through AFM experiments [see

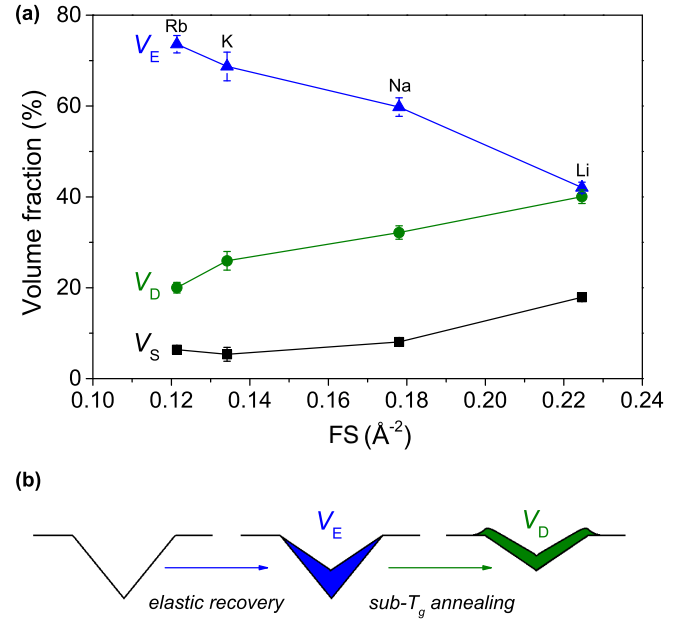


FIG. 8. (a) Alkali field strength (FS) dependence of the elastic ( $V_E$ , blue triangles), densification ( $V_D$ , green circles), and shear flow ( $V_S$ , black squares) volume fractions determined using AFM. (b) Schematic illustration of how  $V_E$  (blue) and  $V_D$  (green) are determined.  $V_S$  is the remaining volume fraction.

Fig. 8(a) and Table IV].  $V_D$  is the product of  $V_R$  and the  $V_i^-/V_G$  ratio, while  $V_S$  is the remaining volume, i.e.,  $1 - (V_D + V_E)$ . Each of these indent volume contributions are schematically illustrated in Fig. 8(b).

By combining the data extracted from AFM, microindentation, and ultrasonic echography, we find that both  $L_D/L_S$  and  $V_E$  exhibit a negative linear scaling with the elastoplastic ratio  $E/H$  (Fig. 9). Hence both quantities provide an estimate of the extent of elastic recovery upon unloading of the indenter. For the present series, glasses with higher FS are less prone to recover elastically and thus more of the supplied mechanical energy is dissipated through plastic deformations. Furthermore, we observe that the decreasing elastic recovery coincides with the FS dependence of  $C_g$  (Fig. 4), yielding an approximately linear relation between  $E/H$  and  $C_g$  (inset of Fig. 9). This correlation is in agreement with that found for other glassy solids. For example, an amorphous silica with a very open network (i.e., low  $C_g$ ) displays a relatively pronounced elastic recovery, while densely packed fluoride glasses generally display a low extent of elastic recovery [9].

The detailed analysis of the indentation deformation mechanisms described above can be summarized as follows: (i) the extent of elastic recovery is decreasing with increasing FS of the modifier, (ii) the shear flow fraction increases with increasing FS even though the overall contribution of this deformation mode is small ( $<18\%$ ), and (iii) higher FS facilitates densification.  $V_R$  has frequently been used to describe the relative contribution of densification to indentation deformation when comparing different glass compositions [18,33,53–55], and in turn linked to the resistance to indentation cracking. The definition of  $V_R$  given in Ref. [33] does not take the

TABLE IV. Indentation and pile-up volumes ( $V_i^-$  and  $V_i^+$ , respectively) for the initial indent; the corresponding volumes after thermal relaxation ( $V_a^-$  and  $V_a^+$ ); volume recovery ratio ( $V_R$ ); elastic, densification, and shear flow volume contributions to full geometrical volume ( $V_E$ ,  $V_D$ , and  $V_S$ , respectively); and ratio of indent diagonal length to the opposite side length ( $L_D/L_S$ ) for the as-prepared glasses. The errors for  $V_i^-$ ,  $V_i^+$ ,  $V_a^-$ ,  $V_a^+$ ,  $V_E$ ,  $V_D$ ,  $V_S$ , and  $L_D/L_S$  do not exceed  $0.8 \mu\text{m}^3$ ,  $0.6 \mu\text{m}^3$ ,  $0.4 \mu\text{m}^3$ ,  $0.6 \mu\text{m}^3$ , 5%, 4%, 3%, 2%, and 0.04, respectively.

Glass ID	$V_i^- (\mu\text{m}^3)$	$V_i^+ (\mu\text{m}^3)$	$V_a^- (\mu\text{m}^3)$	$V_a^+ (\mu\text{m}^3)$	$V_R (\%)$	$V_E (\%)$	$V_D (\%)$	$V_S (\%)$	$L_D/L_S$
Li <sup>a</sup>	13.4	1.2	5.2	2.2	69	42	40	18	1.65
Na <sup>b</sup>	14.1	1.4	3.9	2.5	80	60	32	8	1.72
K	16.2	1.7	4.7	3.6	83	69	26	5	1.82
Rb	15.0	2.5	4.4	2.9	74	74	20	6	1.90

<sup>a</sup>Data are taken from Ref. [24].

<sup>b</sup>Data are taken from Ref. [23].

elastic recovery into account. As a consequence, glasses with substantial elastic recovery can feature high  $V_R$  values due to limited shear flow displacement, but poor resistance to indentation cracking. Hence, we propose that  $V_D$  is a more accurate indicator of a glass's ability to dissipate the indentation-induced stress through densification than  $V_R$ . For the aluminoborate glasses studied herein, we observe that the Li glass is in fact the most efficient in relaxing the largest fraction of  $V_G$  through densification (Fig. 8), whereas it has the lowest  $V_R$  value of the investigated glasses [Fig. 6(a)], which would suggest the opposite conclusion. Therefore, when comparing the deformation mechanism among different compositions, the extent of elastic recovery should be considered as it can affect the result of such comparison. We thus suggest considering  $V_D$ , and not only  $V_R$ , when using AFM studies of indentation imprints to understand the correlation between resistance to indentation cracking and extent of densification.

We also note that the composition dependence of  $V_D$  [Fig. 8(a)] is in good agreement with that of  $\beta$  [Fig. 6(a)] when considering high-FS values, as opposed to  $V_R$ . The reason for higher propensity for densification in high-FS glasses could be due to the higher ability of the small alkali cations to charge balance tetrahedral units than the larger cations, as discussed

in Sec. III. A. Alternatively, the increase in connectivity with increasing FS (Fig. 2) results in a more efficient “locking” of the deformed zone. This agrees well with molecular dynamic simulations, showing that stressed-rigid glasses exhibit lower elastic recovery compared to isostatic glasses [21,56,57]. In other words, a larger fraction of the volume deformed during loading is deformed irreversibly in glasses with higher connectivity. Although this accounts for the composition dependence of  $V_D$  it does not explain why  $\beta$  exhibits a sudden increase with decreasing FS when considering the low-FS glasses such as Cs and Rb. The difference in these two trends may originate from the difference in densification mechanisms taking place at room temperature and  $T_g$ , respectively. Previous work [58] suggests that elevated temperature enables more medium-range order rearrangements, whereas this is strongly limited at ambient temperature.

### F. Indentation cracking

Based on findings in previous studies [9,23,53,59], the extent of indentation-induced densification, Poisson's ratio, and plastic compressibility are all expected to be correlated with the extent and type of indentation cracking. Indeed, when examining the dependence on the probability of crack initiation (CP) at 19.6 N on the FS of the modifying alkali cation, we observe a local maximum around the Na glass [Fig. 10(a)]. The relative length of the cracks with respect to the indent size ( $c/a$  ratio), indicative of the material's brittleness [60], exhibits a strong positive correlation with FS [Fig. 10(a)]. This suggests that the high-FS Li glass is the most brittle of the investigated glasses, while still being able to resist the same load as the low-FS Rb and Cs glasses without cracking. Interestingly, the dependences of CP and  $c/a$  on FS appear to be parallel for all glasses except Li glass, as there is a sharp decrease in CP from the Na to the Li glass. We have also examined the indentation cracking behavior of the compressed glasses. The glasses become less crack resistant and more brittle (i.e., displaying higher  $c/a$  values) upon hot compression (Table V), which is in good agreement with previous work [46] and is presumably due to a decreased ability to densify further during indentation following predensification [61].

Next we combine the information from indentation (crack length and hardness at given load) and ultrasonic echography (elastic modulus) to calculate the indentation fracture toughness ( $K_{Ic}$ ) for the studied series of glasses. It should be noted that indentation testing is not a valid method to calculate

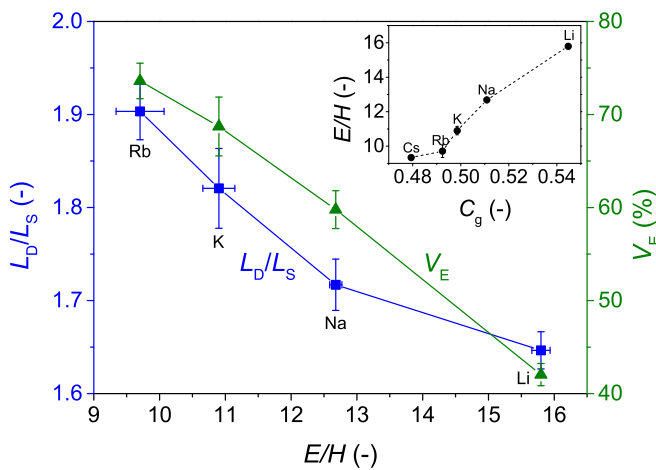


FIG. 9. Dependence of the  $L_D/L_S$  ratio (blue squares) and the elastic volume fraction ( $V_E$ , green triangles) on the elastoplastic ratio ( $E/H$ ). Inset: Correlation between  $E/H$  and atomic packing density ( $C_g$ ).

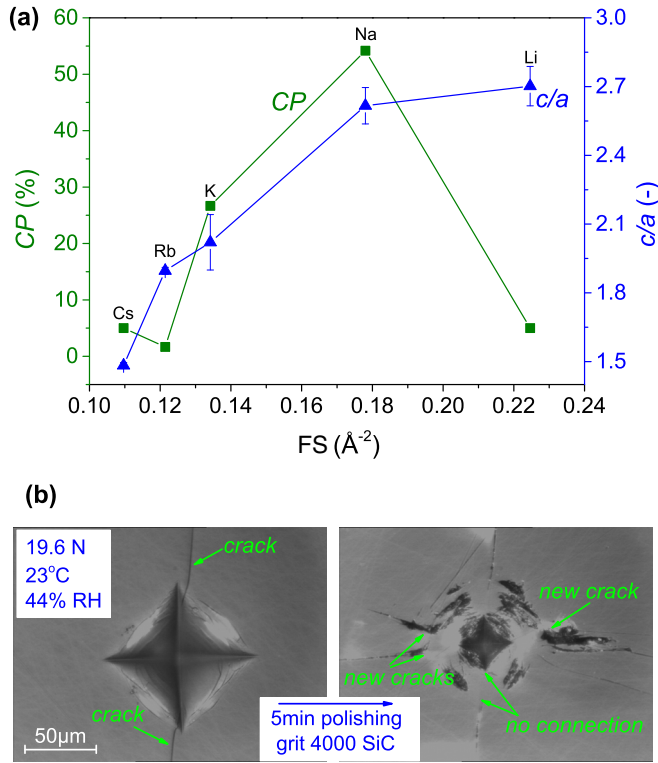


FIG. 10. (a) Alkali field strength (FS) dependence of the crack probability (CP, green squares) and crack-to-indent size ratio ( $c/a$ , blue triangles) at 19.6-N indentation load. Data for Li and Na glasses are taken from Refs. [23,24]. (b) Image of an indent produced at 19.6 N in the Na glass before (left) and after (right) polishing. The radial cracks emanating from the corners of the indent are not connected to the corners of the indent after removal of the original surface. Since there are residual tensile stresses in the vicinity of the noncracked corners of the indent, new cracks appear upon polishing.

fracture toughness, which is a material property [62], and the empirical values of indentation fracture toughness should therefore be treated with caution. That is, the  $K_{Ic}$  values are not necessarily comparable with toughness values obtained through self-consistent methods [63]. This is especially true in the case of the present glasses, which experience significant densification during indentation [64]. However, for the sake of internal comparison, we use indentation testing to estimate

the toughness of these glasses. Depending on the  $c/a$  ratio, one should select the appropriate equation for calculating  $K_{Ic}$ . The equation suggested by Anstis *et al.* [65] [Eq. (13)] should be used if  $c/a > 2.5$ , and the Niihara equation [66] [Eq. (14)] should be used otherwise. The difference in equations is meant to capture the difference in cracking systems, where Eq. (13) is suitable for fully connected median/radial cracks originating below the center of the indent, while Eq. (14) is used for Palmqvist cracks emanating from the corners of the indent [67]:

$$K_{Ic}^{\text{Ans}} = 0.016 \left( \frac{E}{H} \right)^{0.5} \frac{P}{c^{1.5}}, \quad (13)$$

$$K_{Ic}^{\text{Nii}} = 0.018 H^{0.6} E^{0.4} a (c - a)^{-0.5}. \quad (14)$$

For the present glasses, the selection of the appropriate  $K_{Ic}$  equation based on the  $c/a$  value is complicated by the fact that the low-FS glasses exhibit  $c/a < 2.5$ , whereas the high-FS glasses exhibit  $c/a > 2.5$  [Fig. 10(a)]. Therefore, we subject the glasses to mild surface polishing subsequent to indentation in order to look into the type of cracks formed during indentation. The cracks emanating from the corners of an indent produced at 19.6 N in the Na-containing glass [Fig. 10(b)]. This is also found for the other compositions studied herein (images not shown). The fact that the cracks are not connected to the corners of the indent beneath the original surface strongly suggests that the cracking system is of Palmqvist type. This agrees with the expected type of cracking based on Yoffe's indentation stress field [68]. Sellappan *et al.* [9] calculated that there should be no driving force for ring and median indentation cracking at this set of  $\nu$  and  $E/H$  values, while lateral and radial cracking should be expected. Hence, we apply Eq. (14) to calculate the indentation fracture toughness. We observe a minimum in  $K_{Ic}$  for intermediate FS values [Fig. 11(a)]. We note that the trend in  $K_{Ic}$  correlates inversely with that in CP [Fig. 10(a)], indicating that the ability to withstand indentation cracking is correlated to the critical stress intensity for crack propagation within this system, although no one-to-one correlation is observed (not shown). Moreover, we observe that the minimum in  $K_{Ic}$  coincides with that in  $\beta$  [Fig. 6(a)], yielding an approximate positive

TABLE V. Crack probability (CP), crack to half-diagonal length ratio ( $c/a$ ), and indentation fracture toughness calculated according to Eq. (14) ( $K_{Ic}$ ) for as-prepared and compressed glasses measured at 19.6-N indentation load. The estimated errors in CP,  $c/a$ , and  $K_{Ic}$  do not exceed  $\pm 5\%$ , 0.12, and 0.06  $\text{MPa m}^{1/2}$ , respectively.

Glass ID	CP (%)	$c/a$	$K_{Ic}$ ( $\text{MPa m}^{1/2}$ )	CP (%)	$c/a$
	As-prepared			Compressed	
Li <sup>a</sup>	5	2.70	1.26	100	3.54
Na <sup>b</sup>	54	2.62	0.96	99	2.90
K	27	2.02	0.95	88	2.50
Rb	2	1.90	0.94	79	2.81
Cs	5	1.48	1.13	56	2.18

<sup>a</sup>CP and  $c/a$  data are taken from Ref. [24].

<sup>b</sup>CP and  $c/a$  data are taken from Ref. [23].

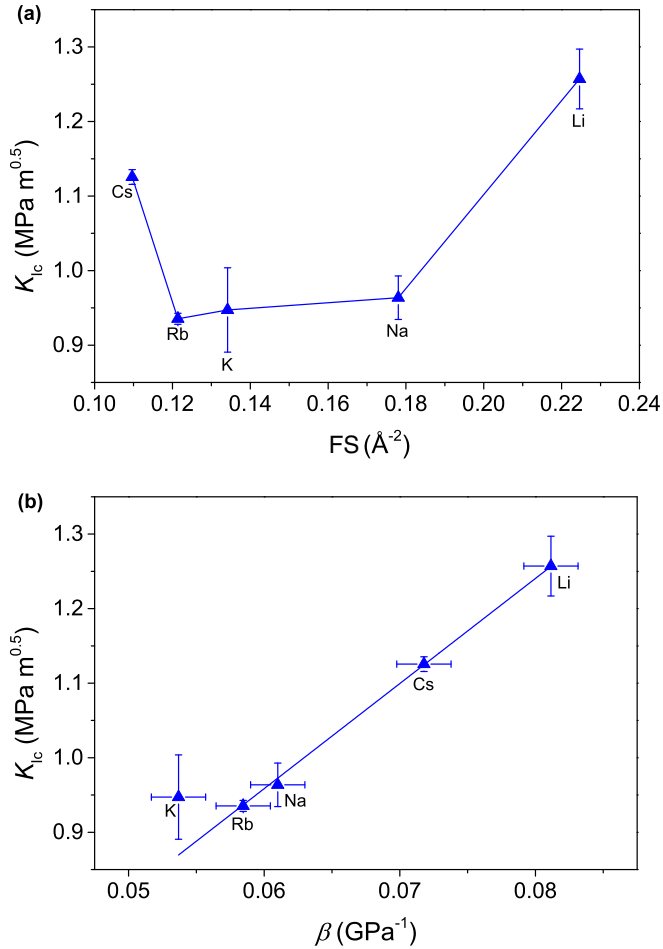


FIG. 11. (a) Alkali field strength (FS) dependence of indentation fracture toughness ( $K_{Ic}$ ) calculated by Niihara's equation [Eq. (14)]. (b) Correlation between  $K_{Ic}$  and plastic compressibility ( $\beta$ ). Errors in  $K_{Ic}$  and  $\beta$  do not exceed  $0.06 \text{ MPa m}^{0.5}$  and  $0.002 \text{ GPa}^{-1}$ , respectively.

linear correlation among these two properties [Fig. 11(b)]. This suggests that  $K_{Ic}$  is controlled by the atomic self-adaptivity introduced in our previous paper [24]. Alternatively, the origin of the minimum in  $K_{Ic}$  is the competition between two effects: (i) decreasing brittleness with increasing FS, in agreement with the trend in  $c/a$  value [Fig. 10(a)], and (ii) increasing fracture surface energy with increasing FS due to stronger alkali-oxygen bonds [69].

#### IV. CONCLUSIONS

We have probed the densification behavior and mechanical properties for a series of slightly peralkaline alkali aluminoborate glasses with varying field strength of the modifying alkali cation. Substitution of the alkali oxide in the glassy network manifests itself in a linear increase in glass transition temperature, hardness, and elastic moduli with increasing field strength, which is explained by the stronger alkali-oxygen bonds. We find that Poisson's ratio surprisingly scales negatively with the atomic packing density, which might be ascribed to the bond strength and the trend in network connectivity. The ratio between densified volume and permanently displaced total indentation volume exhibits a maximum at intermediate modifier field strength, whereas the ratio between densified volume and full geometrical indentation volume shows a linear increase as a function of field strength. This difference in trends shows the importance of considering the elastic recovery during indenter unloading, suggesting that the latter ratio is a more appropriate measure of densification resistance. That is, high modifier field strength glasses are found to exhibit lower resistance to densification, thus dissipating stresses more easily. The indentation fracture toughness displays a minimum at intermediate modifier field strength, which coincides with that found in the extent of densification during hot compression. We suggest that the fracture toughness of the aluminoborate glasses is correlated with the glass's ability to undergo densification-facilitating structural transformations when subjected to pressure, thus dissipating residual stress during indentation.

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